

basic counting principle
 If **event 1 can** occur m different ways and **event 2 can** occur n different ways (after the first has occurred), then the two events can occur $m \cdot n$ ways.
 → Use a decision chart to compute your answer!
 _____ · _____ · _____ · _____

permutation
 an arrangement of items in a certain order where items *cannot be repeated* (such as students sitting in a row of desks.)
 The number of permutations of n objects is $n!$
 $P(n, r)$: the number of permutations of n objects taken r at a time.

$$P(n, r) = \frac{n!}{(n-r)!}$$

distinguishable permutation
 The number of permutations of n objects of which p are alike, q are alike, and r are alike :

$$\frac{n!}{p!q!r!etc.}$$

 repetitions must be accounted for
 be sure to use parentheses around denominator when solving in a calculator!

combination
 the order of the items is not a consideration and items *cannot be repeated* (a combination pizza or a committee of people)

$$C(n, r) = \frac{n!}{r!(n-r)!}$$

independent events do NOT affect each other (rolling dice)
dependent events do affect each other (choosing cards from a deck, no replacement)

Probability

$$P = \frac{\text{\# of desired outcomes}}{\text{total \# of outcomes}}$$

 Sample Space: set of all outcomes

Complements →
 $P(A)$ = probability of event A
 $P(A')$ = prob. of event A not happening

$$P(A) + P(A') = 1$$

intersection of two events
 $P(A \cap B)$
 same as

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

union of two events
 $P(A \cup B) \rightarrow$ same as $P(A \text{ or } B)$
 → mutually exclusive events

Standard deck of playing cards:

- 52 cards → 4 suits (spades, hearts, clubs, diamonds)
- Each suit has 13 cards
- Face cards: Jack, Queen, King
- Aces are low unless stated otherwise (Ace = 1)



cannot happen at the same time

$$P(A \text{ or } B) = P(A) + P(B)$$

 → NOT mutually exclusive
 some objects can satisfy the conditions of both events

$$P(A \text{ or } B) = P(A) + P(B) - P(\text{both})$$

conditional probability
 reduces the sample space since an event has already occurred

$$P(A|B) = \text{The probability of "event A" given "event B."}$$